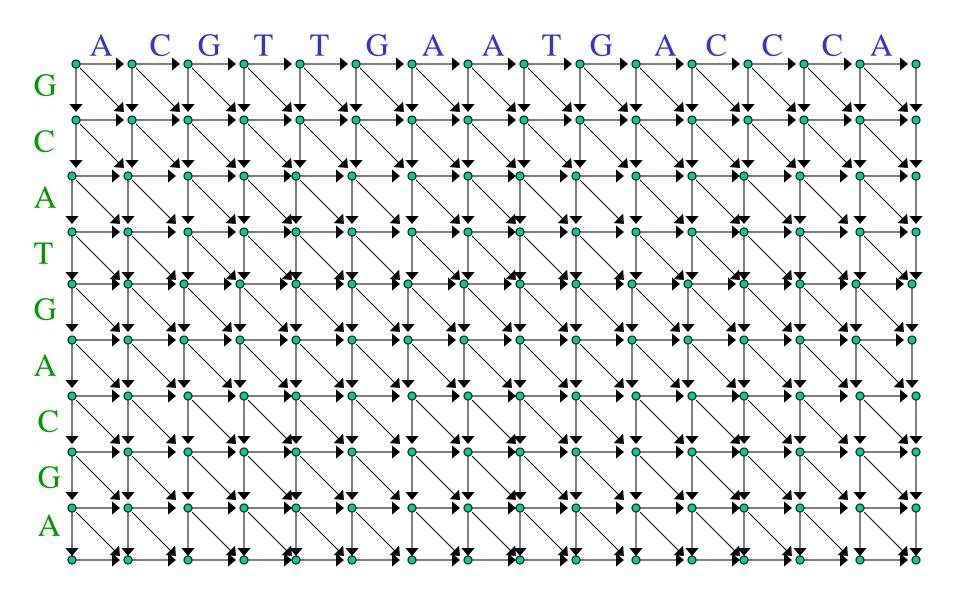
Today's Lecture

• Multiple sequence alignment

- Improved scoring of pairwise alignments
 - Affine gap penalties
 - Profiles

The Edit Graph for a Pair of Sequences

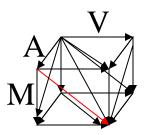


Multiple Alignment via Dynamic Programming

- Higher dimension edit graph
 - each dimension corresponds to a sequence; co-ordinates labelled by residues
 - Each edge corresponds to aligned column of residues (with gaps).
 - Can put arbitrary weights on edges; in particular,
 - can make these correspond to probabilities under an evolutionary model (Sankoff 1975).
 - implicitly assumes independence of columns
- Highest weight path through graph again gives optimal alignment

Generalization to Higher Dimension

Each "cell" in 3-dimensional case looks like this:



Each edge projects onto a gap or residue in each dimension, defining an alignment column; e.g. red edge defines V

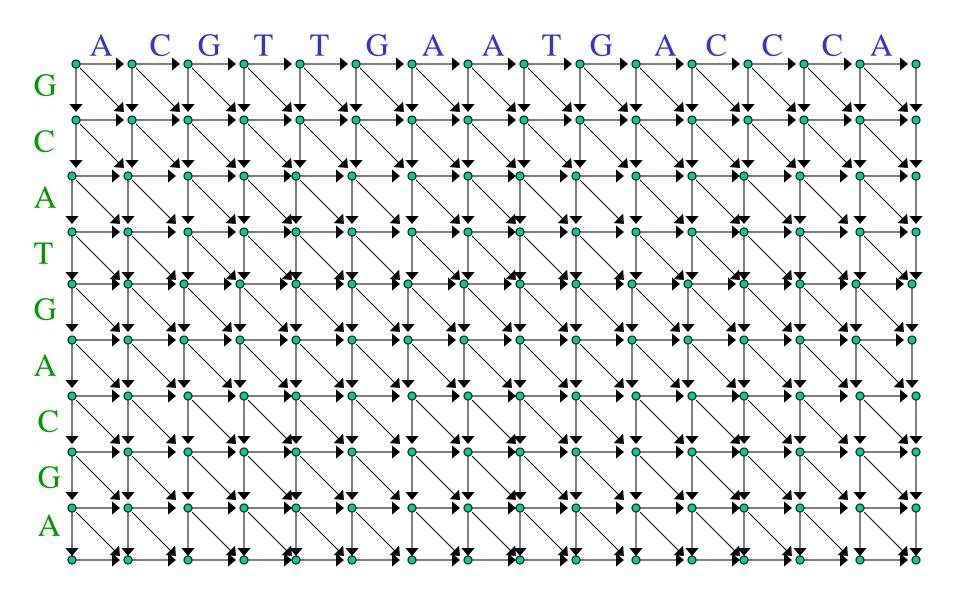
- # edges & # vertices are proportional to product of sequence lengths.
 - For k sequences of size N, is of order $O(N^k)$
 - impractical even for proteins ($N \sim 300$ to 500 residues) if k > 5:

 $300^5 = 2.4 \ 10^{12}$

Multiple alignments: paths in huge WDAGs

- To find high-scoring paths, need to
 - reduce size of graph
 - restrict allowed weighting schemes, and/or
 - sacrifice optimality guarantees
- Durbin *et al.* discuss methods implementing these ideas:
 - Hein
 - Carillo-Lipman
 - progressive alignment (e.g. Clustal)
- HMMs provide nice (but not guaranteed optimal) approach for constructing multiple alignments

The Edit Graph for a Pair of Sequences



Better Scoring Models

- Optimal alignment scoring depends on probabilistic modelling (to be discussed later).
- Inherent limitation of dynamic programming: each alignment column (edge in WDAG) scored independently
 - biologically unrealistic, but
 - required for dynamic programming to work!

- *Two strategies to allow* allow partial non-independence while preserving dynamic programming framework:
 - Enhance graph
 - Allow scores to depend on position within the sequence (i.e. *not* just on a BLOSUM-type score matrix)
 - so some substitutions (of same residues) or gaps penalized more heavily than others

Gap Penalties

TNAVAHVD----DMPNAL YEAAIQLQVTGVVVTDATL

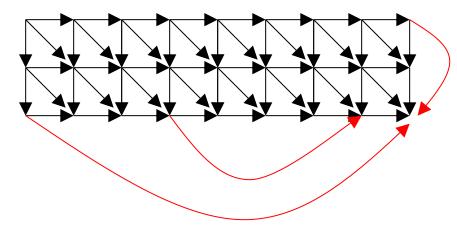
- Usual scoring scheme assigns same penalty *g* to each gap edge, so
 - weights on extended gaps of size s are *linear* in s, i.e.
 - total gap penalty $gap(s) = s \times g$.
 - e.g. in above example, if each g = -6, total penalty on gap would be

$$gap(5) = 5 \times -6 = -30$$

Gap Penalties

- Would like more flexible gap penalties:
- In proteins, insertions & deletions are rare;
 - but when occur, often consist of several residues, because
 - they are in regions (loops) tolerant of length changes
 - at DNA level, indels in protein coding sequence usually a multiple of 3 nucleotides
 - otherwise, would change reading frame
- In noncoding sequence,
 - the most common indel size is 1
 - *but* larger indels occur much more frequently than multiple independent single-base indels

- Can allow arbitrary *convex* gap penalties
 - $-gap(s+t) \ge gap(s) + gap(t)$, where s and t are (integer) gap sizes
 - by extending edit graph:
 - add edges corresponding to *arbitrary length* gaps from each vertex to each horizontally or vertically downstream vertex
 - (convexity condition prevents favoring two adjacent short gaps over a single long gap).
 - Time complexity now O(MN(M+N))
 - often unacceptable for moderate *M*, *N*.
 - Also: how to choose appropriate weights? (need data to estimate!)



Affine Gap Penalties

- *Affine* gap penalties:
 - less general than arbitrary convex penalties, but
 - more general than linear penalties.
- Two parameters:
 - -gap opening penalty g_o
 - -gap extension penalty g_e
- gap(n) (penalty for size n gap) is then

$$g_o + n g_e = g_i + (n-1) g_e$$

where the gap *initiating* penalty $g_i = g_o + g_e$

- Example: for BLOSUM62, good penalties are $-g_i = -12$,
 - $-g_e = -2$

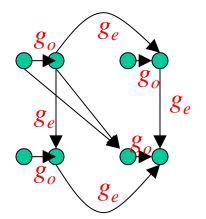
These perform *much* better than linear penalty

- (e.g. g = -6)

- N.B. Durbin *et al.* reverse g_i and g_o - g_i is called the 'gap opening' penalty
- Can obtain affine penalties using extension of edit graph, retaining complexity *O(MN)*:

Edit Graph for Affine Gap Penalties

Double # vertices, creating left-right pair in place of each original vertex. Each cell looks like this:



each left vertex has out-degree and in-degree = 2

each right vertex has out-degree and in-degree = 3

• gap-opening edges from left vertex to right vertex of each pair : weight g_o

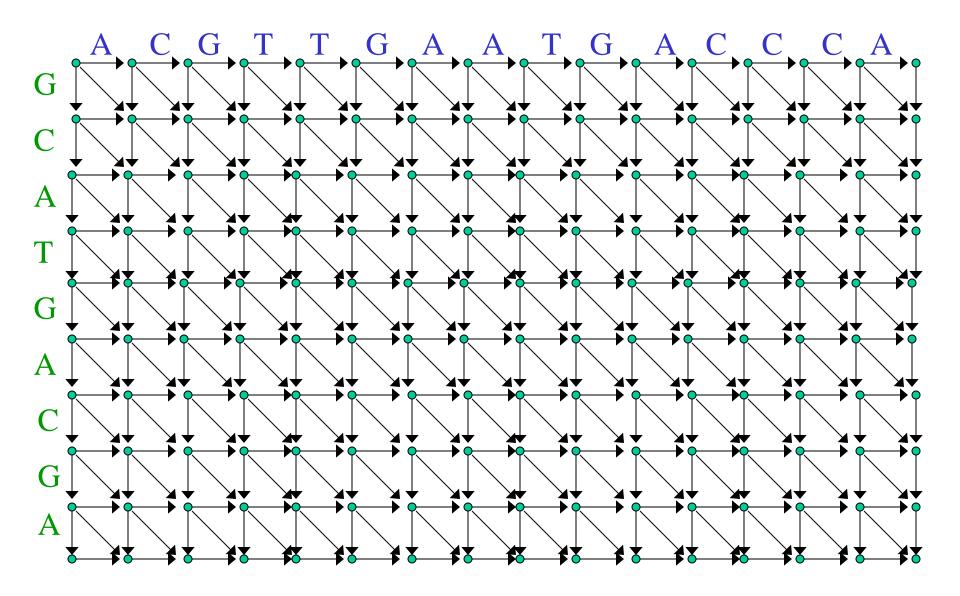
• gap extension edges going horizontally or vertically between right vertices : weight g_e

• diagonal edges originate from either left or right vertex, but always go to a left vertex.

- Paths in the augmented graph still correspond to alignments
 - $\operatorname{can} \exists$ more than one path for same alignment
 - but highest scoring paths still give best alignments
- Score assigned to size *n* gap is g_o + n g_e
 i.e. affine penalty
- Smith-Waterman-Gotoh algorithm

Profiles (position-specific scoring)

The Edit Graph for a Pair of Sequences



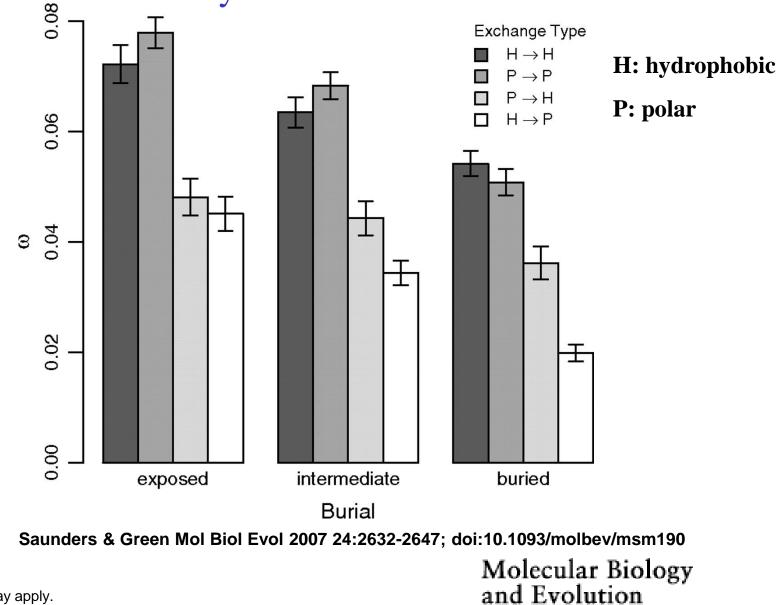
• *Profiles: Position-specific* scoring scheme specifying score of each possible substitution at each position of a sequence

c											
	Cons	A A	С	D	Ε	\mathbf{T}	V	W	Y	Open	Ext
	G	7	-14	- 1	-5	6	4	-34	-22	28	28
1.5	Ρ	5	-26	4	1	1	-4	-48	-31	28	28
	\mathbf{L}	-18	-31	-40	-35	-16	13	-31	-9	100	100
11	T	7	-21	-4	-6	10	-3	-38	-28	100	100
	Е	6	-37	11	12	2	~10	-61	-38	100	100
*	A	5	-34	3	4	1	-8	-48	-34	100	100
	Ε	0	- 53	26	31	-5	-29	-60	-42	100	100
	R	-11	-45	-11	-13	- 3	-21	-2	-33	100	100
	Т	4	-28	-2	-1	8	7	-51	-24	100	100
i –	М	-7	-47	-6	-6	-3	-6	-35	-26	100	100
	V	0	~20	-22	-36	2	41	-56	-27	100	100
1	Х	-9	-44	-1.1	-11	0	-5	-29	-31	100	100
	Ν	5	-27	7	6	8	-11	-40	-32	100	100
	A	7	-27	- 4	-6	4	5	-46	- 3.1	100	100
	W	-47	-69	-58	-60	-40	-49	139	- 6	100	100
	G	11	-31	5	1	3	-5	-65	-43	100	100
	К	- 2	-46	5	8	-1	-23	-49	-45	100	100
	V	- 4	-23	-27	-45	-2	34	-48	-18	100	100
	L	- 3	- 9	-6	-5	-3	З	- 3	-1	26	26
	Ν	-4	-26	3	2	-4	-19	-31	- 9	26	26
	A	4	-16	0	1	2	-12	-40	-10	26	26
	н	Ū	-30	14	10	3	-15	-41	-21	100	100
	I	-2	-20	-18	-23	-1	17	-50	-11	100	100

From R. Luthy, I. Xenarios and P. Bucher, Improving the sensitivity of the sequence profile method *Protein Sci.* 3: 139-146 (1994)

- This is an important improvement!
 - reflects fact that different parts of sequence may evolve at different rates
- e.g. in proteins,
 - internal core region of tightly packed residues, or active sites of enzyme, are more highly conserved;
 - surface residues, particularly in loops, often less conserved.
 - so scores tend to be correlated (high scores in core, lower on surface)

Rates of amino acid exchange in mammalian proteins by burial status



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- PSIBLAST approach:
 - initially compare query sequence to database sequences (using BLOSUM-type scoring matrix),
 - build profile using initial matches
 - rescan database using profile
- Optimal choice of
 - substitution matrix,
 - gap penalties, or
 - profiles

depends on probabilistic modelling (to be discussed later!)